

## **Cambridge O Level**

| CANDIDATE<br>NAME                |                           |                     |  |  |  |  |
|----------------------------------|---------------------------|---------------------|--|--|--|--|
| CENTRE<br>NUMBER                 |                           | CANDIDATE<br>NUMBER |  |  |  |  |
| MATHEMATICS (SYLLABUS D) 4024/21 |                           |                     |  |  |  |  |
| Paper 2 October/November 2020    |                           |                     |  |  |  |  |
|                                  |                           | 2 hours 30 minutes  |  |  |  |  |
| You must answ                    | er on the question paper. |                     |  |  |  |  |
| You will need:                   | Geometrical instruments   |                     |  |  |  |  |

## INSTRUCTIONS

- Answer all questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do **not** use an erasable pen or correction fluid.
- Do **not** write on any bar codes.
- You should use a calculator where appropriate.
- You may use tracing paper.
- You must show all necessary working clearly.
- Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place for angles in degrees, unless a different level of accuracy is specified in the question.
- For  $\pi$ , use either your calculator value or 3.142.

## INFORMATION

- The total mark for this paper is 100.
- The number of marks for each question or part question is shown in brackets [].



1 (a) Here is some information about a holiday.

7-night holiday \$340 per person

8% discount if you book before 31 March

On 15 February, Naseem books this holiday for 2 people.

Calculate the total cost of his holiday.

\$.....[2]

(b) Naseem hires a car for his holiday. The total cost is \$241.50. This cost includes 15% tax.

Calculate the cost of hiring the car excluding tax.

(c) Naseem drives a total of 800 km on holiday. He uses a total of 29.6 litres of fuel.

Calculate the average rate of fuel used in litres per 100 km.

..... litres per 100km [2]

 (d) Naseem changes \$450 to euros (€) for his holiday. The exchange rate between dollars and euros is \$1 = €0.82. On holiday, he spends €297.

Naseem changes the remaining money back to dollars when he returns home. The exchange rate is now 1 = 0.80.

Work out how many dollars he receives.

\$ ...... [3]



2 (a) The cumulative frequency diagram shows the masses, in grams, of 60 potatoes of variety A.

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(b) The table shows the masses, *m* grams, of 120 potatoes of variety C.

| Mass ( <i>m</i> g) | $80 \le m < 100$ | $100 \le m < 120$ | $120 \le m < 130$ | $130 \leqslant m < 140$ | $140 \le m < 200$ |
|--------------------|------------------|-------------------|-------------------|-------------------------|-------------------|
| Frequency          | 10               | 15                | 42                | 36                      | 17                |

Calculate an estimate of the mean mass.

......g [3]

(c) A bag of potatoes has a mass of 2.5 kg, correct to the nearest 100 g. Bags of potatoes are packed into a box. The mass of the box is 600 g, correct to the nearest 10 g.

Calculate the upper bound of the total mass, in kilograms, of a box containing 10 of these bags of potatoes.

- 3 (a) In triangle PQR, PR = 7.5 cm and QR = 6 cm.
  - (i) Using a ruler and compasses only, construct triangle *PQR*. Line *PQ* has been drawn for you.

P Q

[2]

(ii) By taking suitable measurements from your triangle, calculate the area of triangle PQR.



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The diagram shows two triangles. AB = 9.7 cm, BC = 6.4 cm, CD = 3.8 cm and AC = 5.3 cm. $ADC = 63^{\circ}.$ 

(i) Calculate  $D\hat{A}C$ .

 $D\hat{A}C = \dots \qquad [3]$ 

(ii) Calculate  $A\hat{B}C$ .

 $\hat{ABC} = \dots \qquad [3]$ 

4 (a) Complete the table for  $y = \frac{4}{5} \times 2^x$ .

| x | -3 | -2  | -1  | 0   | 1   | 2   | 3   |
|---|----|-----|-----|-----|-----|-----|-----|
| У |    | 0.2 | 0.4 | 0.8 | 1.6 | 3.2 | 6.4 |

**(b)** On the grid, draw the graph of 
$$y = \frac{4}{5} \times 2^x$$
 for  $-3 \le x \le 3$ .



[3]

[1]

(c) By drawing a tangent, estimate the gradient of  $y = \frac{4}{5} \times 2^x$  when x = 2.

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......[2]

(d) Use your graph to estimate the solution of the equation  $4 \times 2^x = 5$ .

x = ..... [1]

10

The diagram shows a garden shed positioned on horizontal ground. It is in the shape of a prism with trapezium *ABCD* as its cross-section. The base of the shed, *ABFE*, is a rectangle. AB = 1.55 m, AD = 2.25 m, BC = 1.85 m and BF = 2.10 m.

(a) Calculate the volume of the shed.

......m<sup>3</sup> [3]



(b) The roof of the shed, *CGHD*, is painted. 1 litre of paint covers 2 square metres.

Calculate the amount of paint used.

..... litres [4]

(c) Calculate the angle of elevation of D from F.

.....[4]

6 (a) Solve the inequality 6x-7 > 5-2x.

......[2]

(b) Chen buys 4 notebooks and 3 pens for \$17.50. Liu buys 2 notebooks and 5 pens for \$14.

Form a pair of simultaneous equations and solve them to find the cost of a notebook and the cost of a pen. Show your working.

Notebook \$ .....

Pen \$ ...... [4]

(c) (i) Show that  $\frac{x}{x+2} - \frac{3}{x-5} = 4$  can be rearranged to  $3x^2 - 4x - 34 = 0$ .

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(ii) Solve the equation  $3x^2 - 4x - 34 = 0$ . Show your working and give your answers correct to 2 decimal places.

 $x = \dots$  or  $x = \dots$  [3]

[3]

7 (a)



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A, B, C and D are points on the circle, centre O.  $B\hat{A}D = 68^{\circ}$  and  $C\hat{B}O = 52^{\circ}$ .

Find CDO.



The cross-section of solid A is the sector of a circle of radius 6 cm and angle  $40^{\circ}$ . The height of solid A is 5 cm.

(i) Calculate the total surface area of solid *A*.

..... cm<sup>2</sup> [4]

(ii) Solid *B* is mathematically similar to solid *A*. The ratio volume of solid A: volume of solid B = 27: 1.

Calculate the surface area of solid *B*.





- 8 A bag contains 36 balls. There are *n* red balls in the bag. The rest of the balls are green. Esther takes two balls from the bag, at random, without replacement.
  - (a) Complete the tree diagram.



- (b) Write an expression, in terms of *n*, for the probability that Esther's first ball is red and her second ball is green.
- (c) The probability that Esther's first ball is red and her second ball is green is  $\frac{1}{7}$ .

Show that  $n^2 - 36n + 180 = 0$ .

(d) Solve the equation  $n^2 - 36n + 180 = 0$ . Show your working.

 $n = \dots$  or  $n = \dots$  [2]

(e) There are more green balls than red balls in the bag.

Find the probability that Esther takes two green balls. Give your answer as a fraction in its lowest terms.

.....[3]

- 9 (a) H is the point (5, 2) and J is the point (-3, 6).
  - (i) Find  $\overrightarrow{HJ}$ .

 $\overrightarrow{HJ} = \left( \begin{array}{c} \\ \end{array} \right) \quad [1]$ 

(ii) Calculate the magnitude of  $\overrightarrow{HJ}$ .

(iii) M is the midpoint of HJ.

Find the position vector of *M*.

[2]



The diagram shows a shape made from seven identical equilateral triangles.  $\overrightarrow{OA} = \mathbf{p}$  and  $\overrightarrow{OF} = \mathbf{q}$ .

- (i) Express, as simply as possible, in terms of **p** and/or **q** 
  - (a)  $\overrightarrow{FB}$ ,

**(b)** 

(b)  $\overrightarrow{FE}$ .

 $\overrightarrow{FE} = \dots \qquad [1]$ 

 $\overrightarrow{FB} = \dots \qquad [1]$ 

(ii) X is a point on FB and FX : XB = 3 : 1.

Express  $\overrightarrow{OX}$ , as simply as possible, in terms of **p** and/or **q**.

 $\overrightarrow{OX} = \dots \qquad [2]$ 

(iii) *Y* is a point on *BD*. Quadrilateral *OXYF* is a trapezium.

Express  $\overrightarrow{XY}$ , as simply as possible, in terms of **p** and/or **q**.

 $\overrightarrow{XY} = \dots \qquad [3]$ 

Question 10 is printed on the next page.

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$$f(x) = \frac{3-2x}{5}$$
  $g(x) = \frac{x-7}{4}$   
(a) Find f(-4).

......[1]

 $f^{-1}(x) = .....$  [3]

(c) g(p) = f(p+1)

(b) Find  $f^{-1}(x)$ .

Find the value of *p*.

p = ..... [3]

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